

Coulomb Interaction:

1) Electric charge \leftrightarrow electron $-e$

a) 2 kinds of charges \swarrow proton $+e$

$$e = 1.6 \times 10^{-19} \text{ C}$$

b) charges are conserved
can't be created singly

\uparrow coulomb

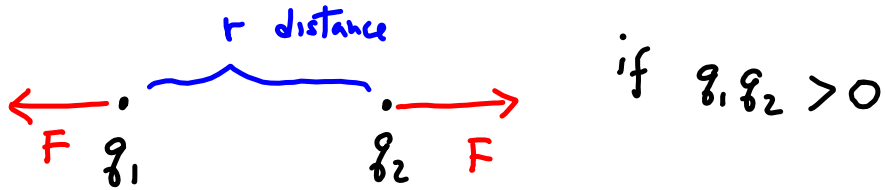
c) charges are quantize

$$e^- + e^+ = 0$$

electron positron photon

$$q = \pm Ne$$

Coulomb interaction between charges



if $q_1 q_2 > 0$

Same charges repulse

$$F = k \frac{|q_1| |q_2|}{r^2}$$

acts along the straight line between the charges
unlike charges attract



if $q_1 q_2 < 0$

$$k = 10^{-7} \frac{\text{C}^2}{\text{N m}^2} \frac{\text{N m}^2}{\text{C}^2}$$

↑
speed of light

← Coulomb

$$k = 10^{-7} 9 \times 10^{16}$$

$$= 9 \times 10^9 \frac{\text{N m}^2}{\text{C}^2}$$

or $8.99 \times 10^9 \text{ N m}^2 / \text{C}^2$

$$c = 2.99792 \times 10^8 \text{ m/s}$$

$$\sim 3 \times 10^8$$

$$\text{Ex 1: } q_1 = 1 \text{ C } \quad q_2 = 1 \text{ C}$$

$$r = 1 \text{ m}$$

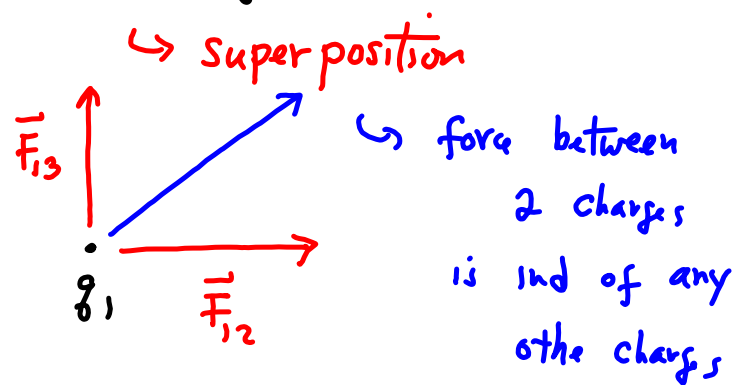
$$F = k \frac{1 \cdot 1}{1^2} = 9 \times 10^9 \text{ N}$$

$$1) \quad 1 \text{ C is } = \frac{1}{4} 9 \times 10^9 \text{ lb} \quad \text{N} \approx 0.22 \text{ lb}$$

a **huge** amount of charge! $\approx (2 \times 10^3) 10^6$ $\sim \frac{1}{4} \text{ lb}$
Ton

$$2) \quad \mu\text{C} = 10^{-6} \text{ C} \quad \text{nC} = 10^{-9} \text{ C}$$

For more than 2 charges

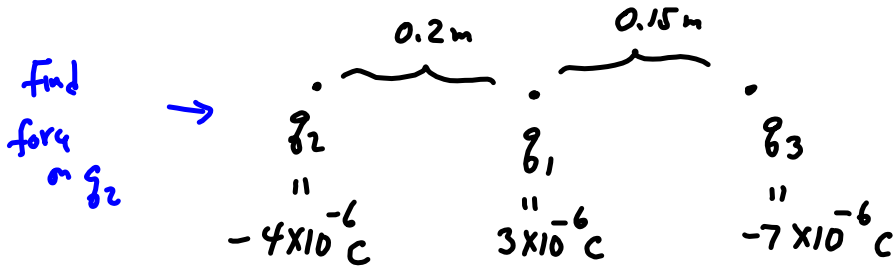


The force exerted by q_2 on q_1 is F_{12} on 1 by 2

q_3 $\vec{F}_1 = \vec{F}_{12} + \vec{F}_{13}$

$$\vec{F}_1 = \vec{F}_{12} + \vec{F}_{13} + \vec{F}_{14} + \vec{F}_{15} + \dots$$

Ex 2 three charges on a line



Find the total force on q_1

$$F_{13} = k \frac{|q_1||q_3|}{(0.15)^2} = \frac{9 \times 10^9 \cdot 3 \times 10^{-6} \cdot 7 \times 10^{-6}}{(0.15)^2}$$

$$= \frac{9 \times 3 \times 7 \times 10^{-3}}{2.25 \times 10^{-2}} = \frac{1.5 \times 10^{-1}}{(1.5)^2 \cdot 10^{-2}} = \frac{9 \times 21}{2.25} \cdot 10^{-1} = 8.4 \text{ N}$$

$$F_{12} = k \frac{|q_1||q_2|}{(0.2)^2} = \frac{9 \times 10^9 \cdot 3 \times 10^{-6} \cdot 4 \times 10^{-6}}{4 \times 10^{-2}} = \frac{9 \cdot 3 \cdot 4}{4} \cdot 10^{-1} = 2.7 \text{ N}$$

$$\vec{F}_1 = \vec{F}_{12} + \vec{F}_{13}$$

$$= -2.7 \text{ N} + 8.4 \text{ N}$$

$$= 5.7 \text{ N}$$

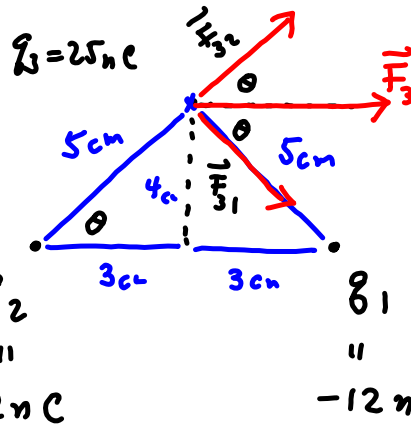
Your turn: What is the force on q_2 due to $q_1 + q_3$?

- A) 4.8 N
- B) -0.6 N
- C) -4.8 N
- D) 0.6 N ✓

$$F_{21} = F_{12} = 2.7 \quad F_{23} = 2.1 \quad \vec{F}_2 = \vec{F}_{21} + \vec{F}_{23}$$

$$= 2.7 - 2.1 = 0.6 \text{ N}$$

Ex 3 :



Find the total force on q_3

$q_1 + q_2$ forms dipole

$a = 10^{-2} m$

$$\vec{F}_3 = \vec{F}_{32} + \vec{F}_{31}$$

$$F_{32} = k \frac{|q_3| |q_2|}{(5 \times 10^{-2})^2} = \frac{9 \times 10^9 \cdot 25 \times 10^{-9} \cdot 12 \times 10^{-9}}{25 \times 10^{-4}}$$

$$= \frac{9 \cdot 25 \cdot 12 \cdot 10^{-9}}{25 \cdot 10^{-4}} = 108 \times 10^{-5} = 1.08 \times 10^{-3} N$$

$$F_{31} = 1.08 \times 10^{-3} N$$

$$F_3 = F_{32x} + F_{31x}$$

$$= F_{32} \cos \theta + F_{31} \cos \theta = 1.08 \times 10^{-3} N \cdot 2 \cos \theta$$

$$\cos \theta = \frac{3}{5}$$

$$= 1.08 \times 10^{-3} \cdot 2 \cdot \frac{3}{5} = \underline{\underline{1.3 \times 10^{-3} N}}$$

What is force on $q_3 = -25 nC$?

- A up
- B down
- C to the left
 $-1.3 \times 10^{-3} N$
- D to the right