

Homework 1. Due whatever day you decide to have the homework session.

Problem 1. *Rising Snake*

A snake of length L and linear mass density ρ rises from the table. Its head is moving straight up with the constant velocity v . What force does the snake exert on the table?

Problem 2. *1983-Spring-CM-U-1.*

A ball, mass m , hangs by a massless string from the ceiling of a car in a passenger train. At time t the train has velocity \vec{v} and acceleration \vec{a} in the same direction. What is the angle that the string makes with the vertical? Make a sketch which clearly indicates the relative direction of deflection.

Problem 3. *1984-Fall-CM-U-1.*

Sand drops vertically from a stationary hopper at a rate of 100 gm/sec onto a horizontal conveyor belt moving at a constant velocity, \vec{v} , of 10 cm/sec.

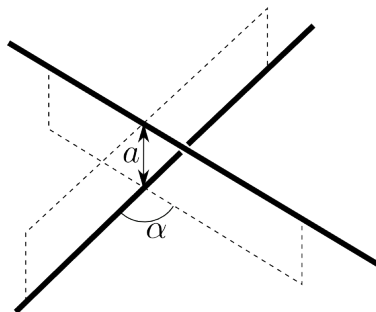
1. What force (magnitude and direction relative to the velocity) is required to keep the belt moving at a constant speed of 10 cm/sec?
2. How much work is done by this force in 1.0 second?
3. What is the change in kinetic energy of the conveyor belt in 1.0 second due to the additional sand on it?
4. Should the answers to parts 2. and 3. be the same? Explain.

Problem 4. *1994-Fall-CM-U-1*

Two uniform very long (infinite) rods with identical linear mass density ρ do not intersect. Their directions form an angle α and their shortest separation is a .

1. Find the force of attraction between them due to Newton's law of gravity.
2. Give a dimensional argument to explain why the force is independent of a .
3. If the rods were of a large but finite length L , what dimensional form would the lowest order correction to the force you found in the first part have?

Note: for $A^2 < 1$, $\int_{-\pi/2}^{\pi/2} \frac{d\theta}{1-A^2 \sin^2 \theta} = \frac{\pi}{\sqrt{1-A^2}}$



Homework 2. Due Wednesday, February 01

Problem 1. 1985-Spring-CM-U-3.

A damped one-dimensional linear oscillator is subjected to a periodic driving force described by a function $F(t)$. The equation of motion of the oscillator is given by

$$m\ddot{x} + b\dot{x} + kx = F(t),$$

where $F(t)$ is given by

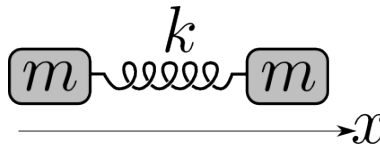
$$F(t) = F_0 (1 + \sin(\omega t)).$$

The driving force frequency is $\omega = \omega_0$ and the damping by $b/2m = \omega_0$, where $\omega_0^2 = k/m$. At $t = 0$ the mass is at rest at the equilibrium position, so that the initial conditions are given by $x(0) = 0$, and $\dot{x}(0) = 0$. Find the solution $x(t)$ for the position of the oscillator vs. time.

Problem 2. 1989-Fall-CM-U-1.

Two equal masses m are connected by a string of force constant k . They are restricted to motion in the \hat{x} direction.

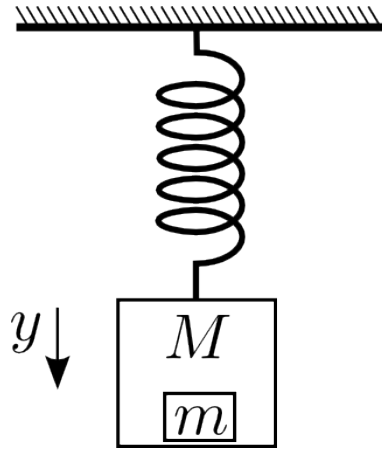
1. Find the normal mode frequencies.
2. A leftward impulse P is suddenly given to the particle on the right. How long does it take for the spring to reach maximum compression?
3. How far does the mass on the left travel before the spring reaches maximum compression?



Problem 3. 2001-Spring-CM-G-5

An ideal massless spring hangs vertically from a fixed horizontal support. A block of mass m rests on the bottom of a box of mass M and this system of masses is hung on the spring and allowed to come to rest in equilibrium under the force of gravity. In this condition of equilibrium the extension of the spring beyond its relaxed length is Δy . The coordinate y as shown in the figure measures the displacement of M and m from equilibrium.

1. Suppose the system of two masses is raised to a position $y = -d$ and released from rest at $t = 0$. Find an expression for $y(t)$ which correctly describes the motion for $t \geq 0$.
2. For the motion described in the previous part, determine an expression for the force of M on m as a function of time.
3. For what value of d is the force on m by M instantaneously zero immediately after m and M are released from rest at $y = -d$?



Homework 3. Due Wednesday, February 8

Problem 1. *1984-Fall-CM-U-2.*

Two forces \mathbf{F}^A and \mathbf{F}^B have the following components

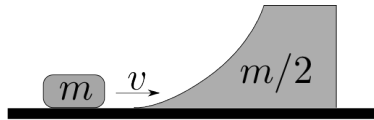
$$\mathbf{F}^A : \begin{cases} F_x^A = 6abyz^3 - 20bx^3y^2 \\ F_y^A = 6abxz^3 - 10bx^4y \\ F_z^A = 18abxyz^2 \end{cases}, \quad \mathbf{F}^B : \begin{cases} F_x^B = 18abyz^3 - 20bx^3y^2 \\ F_y^B = 18abxz^3 - 10bx^4y \\ F_z^B = 6abxyz^2 \end{cases}$$

Which one of these is a conservative force? Prove your answer. For the conservative force determine the potential energy function $V(x, y, z)$. Assume $V(0, 0, 0) = 0$.

Problem 2. *1987-Fall-CM-U-1.*

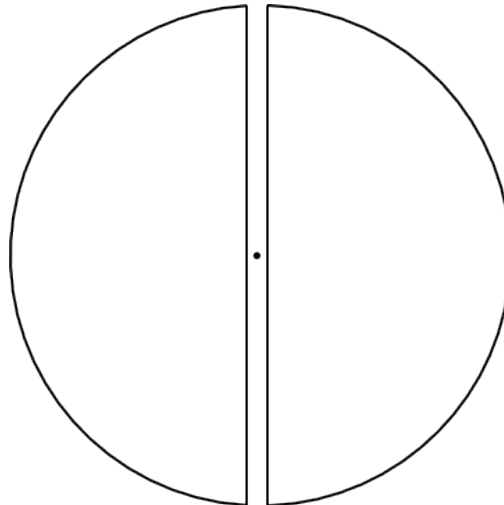
A block of mass m slides on a frictionless table with velocity v . At $x = 0$, it encounters a frictionless ramp of mass $m/2$ which is sitting at rest on the frictionless table. The block slides up the ramp, reaches maximum height, and slides back down.

1. What is the velocity of the block when it reaches its maximum height?
2. How high above the frictionless table does the block rise?
3. What are the final velocities of the block and the ramp?



Problem 3. *1983-Fall-CM-G-5*

Assume that the earth is a sphere, radius R and uniform mass density, ρ . Suppose a shaft were drilled all the way through the center of the earth from the north pole to the south. Suppose now a bullet of mass m is fired from the center of the earth, with velocity v_0 up the shaft. Assuming the bullet goes beyond the earth's surface, calculate how far it will go before it stops.



Problem 4. *1995-Spring-CM-G-2.jpg*

A particle of mass m moves under the influence of a central attractive force

$$F = -\frac{k}{r^2}e^{-r/a}$$

1. Determine the condition on the constant a such that circular motion of a given radius r_0 will be stable.
2. Compute the frequency of small oscillations about such a stable circular motion.

Homework 4. Due Wednesday, February 15

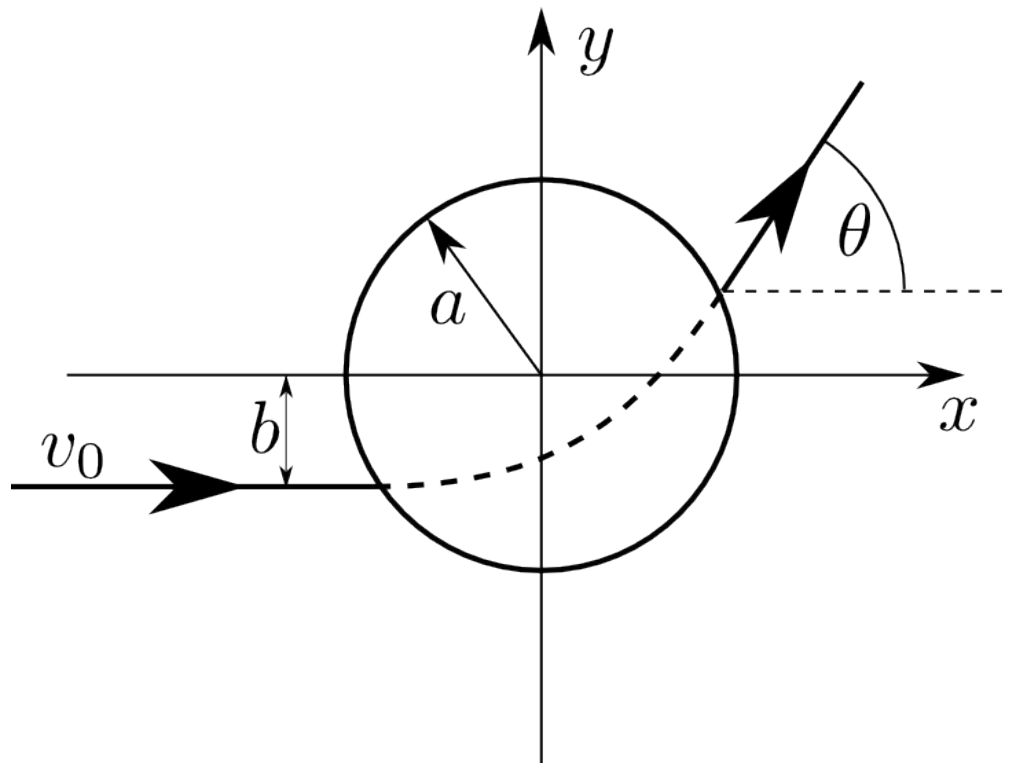
Problem 1. 2001-Spring-CM-U-3

A particle with mass m , confined to a plane, is subject to a force field given by

$$\vec{F}(\vec{r}) = \begin{cases} -k\vec{r}, & \text{for } |r| \leq a \\ 0, & \text{for } |r| > a \end{cases}$$

The particle enters the field from the left horizontally with an initial velocity v_0 and a distance $b < a$ below the force center as shown.

1. Write down the equation of motion for $r \leq a$ in Cartesian coordinates in terms of x , y , and $\omega = \sqrt{k/m}$
2. Give the trajectory of the particle when $r < a$.
3. For $v_0 = a\omega$ find the coordinates of the particle as it exits the region of non-zero force field.
4. For $v_0 = a\omega$, find the deflection angle θ of the departing velocity at the exit point.



Problem 2. 1998-Spring-CM-U-3

A particle of mass m has velocity v_0 when it is far from the center of a potential of the form:

$$V(r) = \frac{k}{r^4},$$

where k is a positive constant that you can conveniently write as

$$k = \frac{1}{2}mv_0^2a^4.$$

1. Find r_{min} the distance of the closest approach of the particle to the center of force, as a function of the impact parameter b of the particle.
2. Find an expression for the scattering angle of the particle as a function of the impact parameter b . Your expression may include a definite integral that you need not evaluate, so long as no unknown quantities appear in the integral.



Problem 3. 1994-Fall-CM-G-3.jpg

A particle of mass m moves under the influence of an attractive central force $F(r) = -k/r^3$, $k > 0$. Far from the center of force, the particle has a kinetic energy E .

1. Find the values of the impact parameter b for which the particle reaches $r = 0$.
2. Assume that the initial conditions are such that the particle misses $r = 0$. Solve for the scattering angle θ_s , as a function of E and the impact parameter b .

Problem 4.

1. Determine the cross-section for a particle of energy E to “fall” to the center of a field $U = -\frac{\alpha}{r^2}$, where $\alpha > 0$.
2. Determine the cross-section for a particle of energy E to “fall” to the center of a field $U = -\frac{\alpha}{r^n}$, where $\alpha > 0$ and $n > 2$.

Homework 5. Due Wednesday, February 22

Problem 1. *A string with a tension*

A string of tension T and linear mass density ρ connects two horizontal points distance L apart from each other. y is the vertical coordinate pointing up, and x the is horizontal coordinate.

1. Write down the functional of potential energy of the string vs. the shape of the string $y(x)$. Specify the boundary conditions for the function $y(x)$.
2. Write down the equation which gives the shape of minimal energy for the string.
3. Find the solution of the equation which satisfies the boundary conditions. (Do not try to solve the transcendental equation for one of the constant. Just write it down.)
4. In the case $T \gg \rho gL$, the shape is approximately given by $y \approx -\frac{\alpha}{2}x(L-x)$. Find α .

Problem 2. *1995-Spring-CM-G-3*

A soap film is stretched over 2 coaxial circular loops of radius R , separated by a distance $2H$. Surface tension (energy per unit area, or force per unit length) in the film is $\tau = \text{const}$. Gravity is neglected.

1. Assuming that the soap film takes an axisymmetric shape, such as illustrated in the figure, find the equation for $r(z)$ of the soap film, with r_0 (shown in the figure) as the only parameter. (Hint: You may use either variational calculus or a simple balance of forces to get a differential equation for $r(z)$).
2. Write a transcendental equation relating r_0 , R and H , determine approximately and graphically the maximum ratio $(H/R)_c$, for which a solution of the first part exists. If you find that multiple solutions exist when $H/R < (H/R)_c$, use a good physical argument to pick out the physically acceptable one.
3. What shape does the soap film assume for $H/R > (H/R)_c$?

Problem 3. *1987-Fall-CM-G-4*

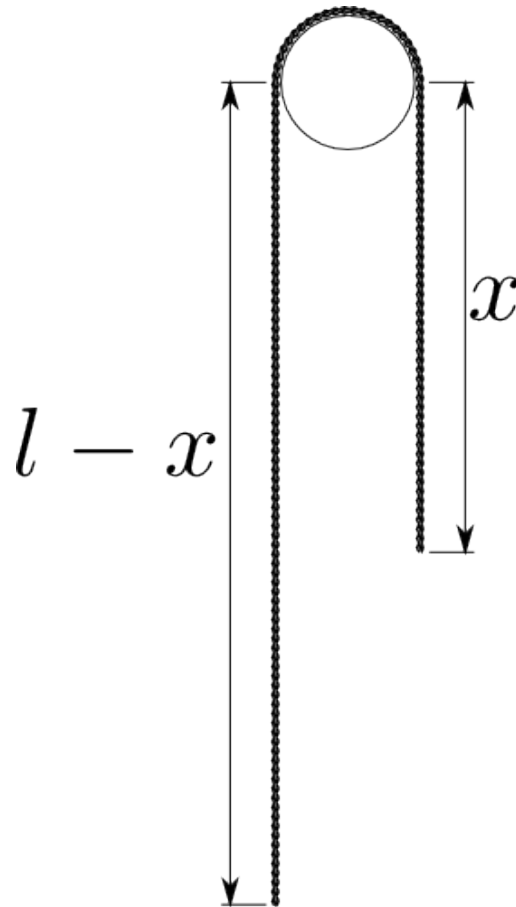
Assume that the sun (mass M_\odot) is surrounded by a uniform spherical cloud of dust of density ρ . A planet of mass m moves in an orbit around the sun within the dust cloud. Neglect collisions between the planet and the dust.

1. What is the angular velocity of the planet when it moves in a circular orbit of radius r ?
2. Show that if the mass of the dust within the sphere of the radius r is small compared to M_\odot , a nearly circular orbit will precess. Find the angular velocity of the precession.

Homework 6. Due Wednesday, March 1.

Problem 1. 1983-Spring-CM-G-4

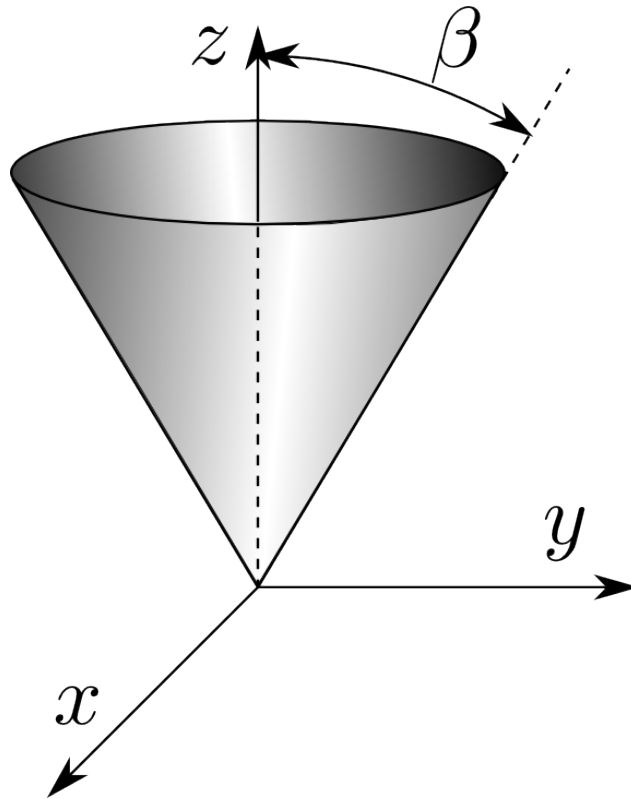
A simple Atwood's machine consists of a heavy rope of length l and linear density ρ hung over a pulley. Neglecting the part of the rope in contact with the pulley, write down the Lagrangian. Determine the equation of motion and solve it. If the initial conditions are $\dot{x} = 0$ and $x = l/2$, does your solution give the expected result?



Problem 2. 1993-Spring-CM-G-5.jpg

Consider a particle of mass m constrained to move on the surface of a cone of half angle β , subject to a gravitational force in the negative z -direction. (See figure.)

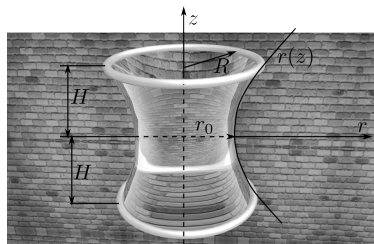
1. Construct the Lagrangian in terms of two generalized coordinates and their time derivatives.
2. Calculate the equations of motion for the particle.
3. Show that the Lagrangian is invariant under rotations around the z -axis, and, calculate the corresponding conserved quantity.



Problem 3. *May the Force be with you*

A soap film is stretched over 2 coaxial circular loops of radius R , separated by a distance $2H$. Surface tension (energy per unit area, or force per unit length) in the film is $\tau = \text{const}$. Gravity is neglected.

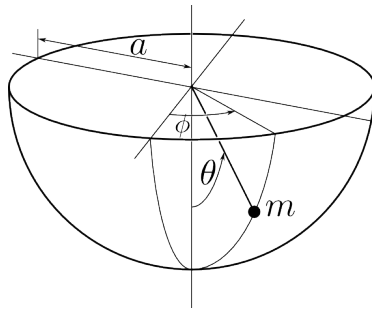
1. Assuming that the soap film takes an axisymmetric shape, such as illustrated in the figure, find the equation for $r(z)$ of the soap film, with r_0 (shown in the figure) as the only parameter. (Hint: You may use either variational calculus or a simple balance of forces to get a differential equation for $r(z)$).
2. Write a transcendental equation relating r_0 , R and H , determine approximately and graphically the maximum ratio $(H/R)_c$, for which a solution of the first part exists. If you find that multiple solutions exist when $H/R < (H/R)_c$, use a good physical argument to pick out the physically acceptable one.
3. Compute the force required to hold the loops apart at distance H .



Problem 4. 1996-Fall-CM-G-4

A particle of mass m slides inside a smooth hemispherical cup under the influence of gravity, as illustrated. The cup has radius a . The particle's angular position is determined by polar angle θ (measured from the negative vertical axis) and azimuthal angle ϕ .

1. Write down the Lagrangian for the particle and identify two conserved quantities.
2. Find a solution where $\theta = \theta_0$ is constant and determine the angular frequency $\dot{\phi} = \omega_0$ for the motion.
3. Now suppose that the particle is disturbed slightly so that $\theta = \theta_0 + \alpha$ and $\dot{\phi} = \omega_0 + \beta$, where α and β are small time-dependent quantities. Obtain, to linear order in α and β the equations of motion for the perturbed motion. Hence find the frequency of the small oscillation in θ that the particle undergoes.



Homework 7. Due Wednesday, March 8

Problem 1. 1992-Spring-CM-G-5

A particle of mass m is moving on a sphere of radius a , in the presence of a velocity dependent potential $U = \sum_{i=1,2} \dot{q}_i A_i$, where $q_1 = \theta$ and $q_2 = \phi$ are the generalized coordinates of the particle and $A_1 \equiv A_\theta$, $A_2 \equiv A_\phi$ are given functions of θ and ϕ .

1. Calculate the generalized force defined by

$$Q_i = \frac{d}{dt} \frac{\partial U}{\partial \dot{q}_i} - \frac{\partial U}{\partial q_i}.$$

2. Write down the Lagrangian and derive the equation of motion in terms of θ and ϕ .
3. For $A_\theta = 0$, $A_\phi = \frac{g}{a} \frac{1 - \cos \theta}{\sin \theta}$, where g is a constant, describe the symmetry of the Lagrangian and find the corresponding conserved quantity. (Can you figure out what is the magnetic field in this case?)
4. In terms of three dimensional Cartesian coordinates, *i.e.*, $q_i = x_i$ show that Q_i can be written as $\vec{Q} = \vec{v} \times \vec{B}$, where $v_i = \dot{x}_i$. Find \vec{B} in terms of \vec{A} .

Problem 2. 1999-Spring-CM-G-4.jpg

A particle of mass m is observed to move in a central field following a planar orbit (in the $x - y$ plane) given by.

$$r = r_0 e^{-\theta},$$

where r and θ are coordinates of the particle in a polar coordinate system.

1. Prove that, at any instant in time, the particle trajectory is at an angle of 45° to the radial vector.
2. When the particle is at $r = r_0$ it is seen to have an angular velocity $\Omega > 0$. Find the total energy of the particle and the potential energy function $V(r)$, assuming that $V \rightarrow 0$ as $r \rightarrow +\infty$.
3. Determine how long it will take the particle to spiral in from $r = r_0$, to $r = 0$.

Problem 3. Noether's theorem

Which components (or their combinations) of momentum \vec{P} and angular momentum \vec{M} are conserved in motion in the following fields.

1. the field of an infinite homogeneous plane,
2. that of an infinite homogeneous cylinder,
3. that of an infinite homogeneous prism,
4. that of two points,

5. that of an infinite homogeneous half plane,
6. that of a homogeneous cone,
7. that of a homogeneous circular torus,
8. that of an infinite homogeneous cylindrical helix of pitch h .

Homework 8. Due Wednesday, March 22

Problem 1. 1985-Spring-CM-G-5

A bead slides without friction on a wire in the shape of a cycloid:

$$x = a(\theta - \sin \theta)$$

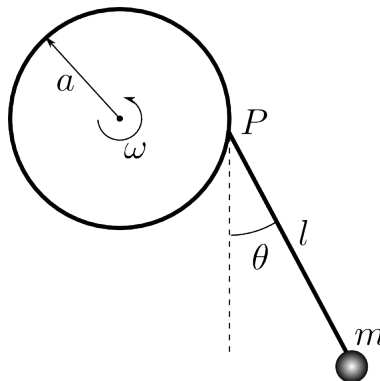
$$y = a(1 + \cos \theta)$$

1. Write down the Hamiltonian of the system.
2. Derive Hamiltonian's equations of motion.

Problem 2. 1991-Fall-CM-G-5

A simple pendulum of length l and mass m is suspended from a point P that rotates with constant angular velocity ω along the circumference of a vertical circle of radius a .

1. Find the Hamiltonian function and the Hamiltonian equation of motion for this system using the angle θ as the generalized coordinate.
2. Do the canonical momentum conjugate to θ and the Hamiltonian function in this case correspond to physical quantities? If so, what are they?



Problem 3. 1991-Spring-CM-G-5

A particle is constrained to move on a cylindrically symmetric surface of the form $z = (x^2 + y^2)/(2a)$. The gravitational force acts in the $-z$ direction.

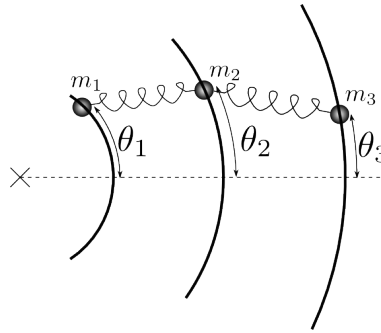
1. Use generalized coordinates with cylindrical symmetry to incorporate the constraint and derive the Lagrangian for this system.
2. Derive the Hamiltonian function, Hamilton's equation, and identify any conserved quantity and first integral of motion.
3. Find the radius r_0 of a steady state motion in r having angular momentum l .
4. Find the frequency of small radial oscillations about this steady state.

Homework 9. Due Wednesday, March 29

Problem 1. 1991-Spring-CM-G-4

Three particles of masses $m_1 = m_0$, $m_2 = m_0$, and $m_3 = m_0/3$ are restricted to move in circles of radius a , $2a$, and $3a$ respectively. Two ideal springs of natural length much smaller than a and force constant k link particles 1, 2 and particles 2, 3 as shown.

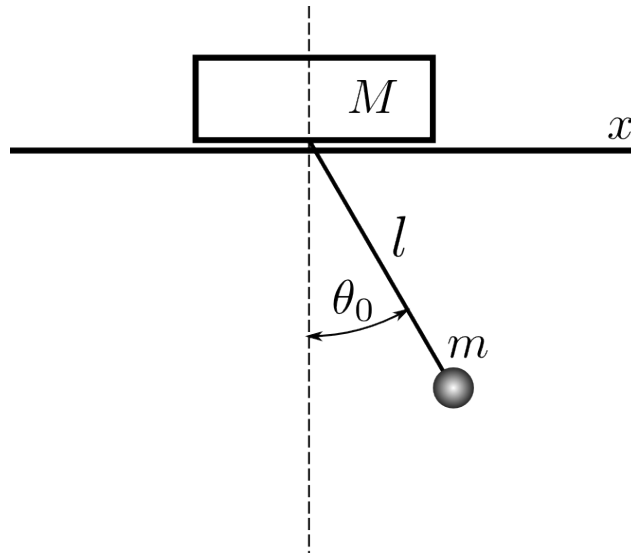
1. Determine the Lagrangian of this system in terms of polar angles θ_1 , θ_2 , θ_3 and parameters m_0 , a , and k .
2. For small oscillations about an equilibrium position, determine the system's normal mode frequencies in term of $\omega_0 = \sqrt{k/m_0}$.
3. Determine the normalized eigenvector corresponding to each normal mode and describe their motion physically.
4. What will happen if the natural length of the springs is a ?



Problem 2. 1994-Spring-CM-G-3.jpg

A simple pendulum of length l and mass m is attached to a block of mass M , which is free to slide without friction in a horizontal direction. All motion is confined to a plane. The pendulum is displaced by a small angle θ_0 and released.

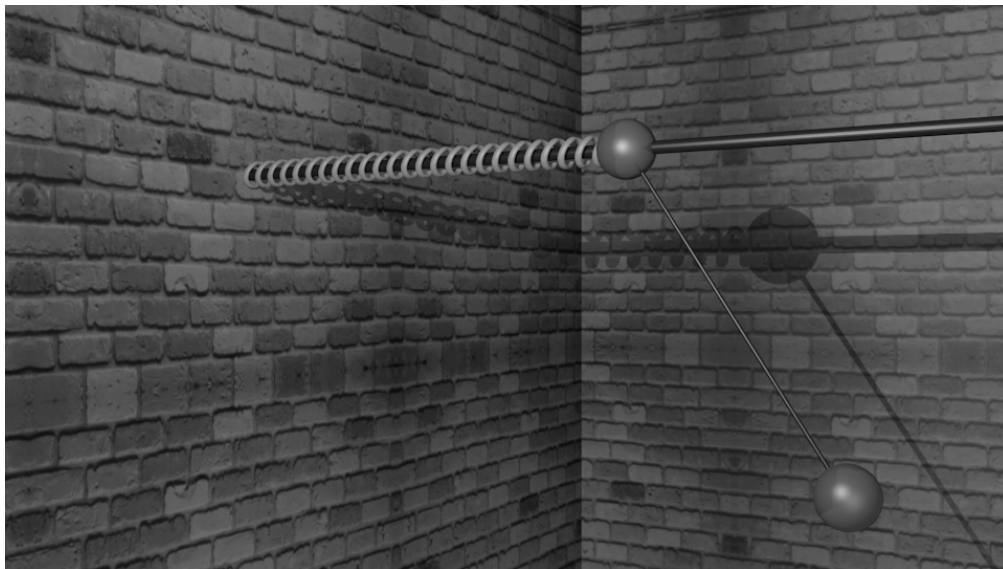
1. Choose a convenient set of generalized coordinates and obtain Lagrange's equations of motion. What are the constants of motion?
2. Make the small angle approximation ($\sin \theta \approx \theta$, $\cos \theta \approx 1$) and solve the equations of motion. What is the frequency of oscillation of the pendulum, and what is the magnitude of the maximum displacement of the block from its initial position?



Problem 3. *1995-Fall-CM-G-1.jpg*

Consider a system of two point-like weights, each of mass M , connected by a massless rigid rod of length l . The upper weight slides on a horizontal frictionless rail and is connected to a horizontal spring, with spring constant k , whose other end is fixed to a wall as shown below. The lower weight swings on the rod, attached to the upper weight and its motion is confined to the vertical plane.

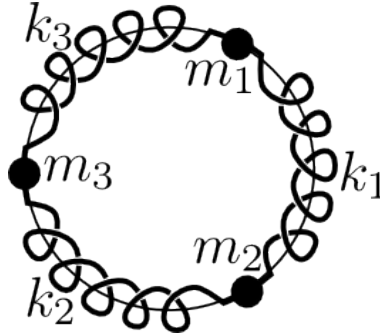
1. Find the exact equations of motion of the system.
2. Find the frequencies of small amplitude oscillation of the system.
3. Describe qualitatively the modes of small oscillations associated with the frequencies you found in the previous part.



Homework 10. Due Wednesday, April 5

Problem 1. 1985-Fall-CM-U-3.

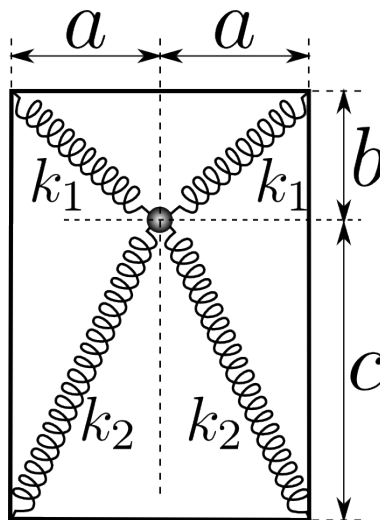
Three particles of the same mass $m_1 = m_2 = m_3 = m$ are constrained to move in a common circular path. They are connected by three identical springs of stiffness $k_1 = k_2 = k_3 = k$, as shown. Find the normal frequencies and normal modes of the system.



Problem 2. 1991-Fall-CM-U-2.

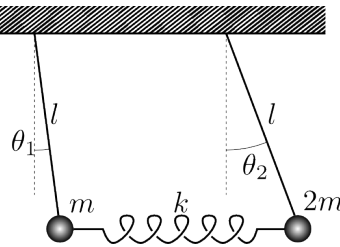
A steel ball of mass M is attached by massless springs to four corners of a $2a$ by $b+c$ horizontal, rectangular frame. The springs constants k_1 and k_2 with corresponding equilibrium lengths $L_1 = \sqrt{a^2 + b^2}$ and $L_2 = \sqrt{a^2 + c^2}$ as shown. Neglecting the force of gravity,

1. Find the frequencies of small amplitude oscillations of the steel ball in the plane of rectangular frame.
2. Identify the type of motion associated with each frequency.
3. Is the oscillation of the steel ball perpendicular to the plane of the rectangular frame harmonic? Why or why not?



Problem 3. 1983-Spring-CM-G-6

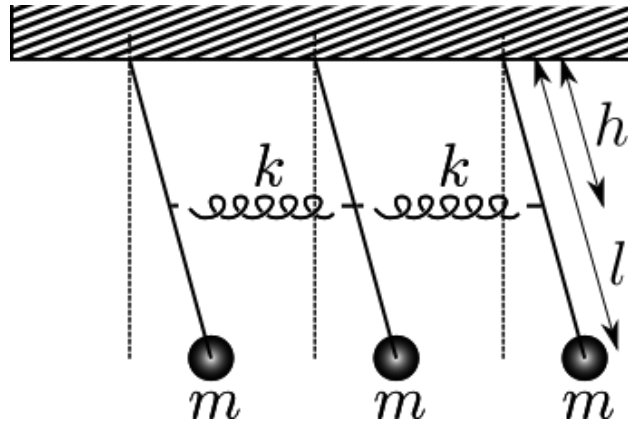
Two pendula made with massless strings of length l and masses m and $2m$ respectively are hung from the ceiling. The two masses are also connected by a massless spring with spring constant k . When the pendula are vertical the spring is relaxed. What are the frequencies for small oscillations about the equilibrium position? Determine the eigenvectors. How should you initially displace the pendula so that when they are released, only one eigen frequency is excited. Make the sketches to specify these initial positions for both eigen frequencies.



Homework 11. Due Wednesday, April 12

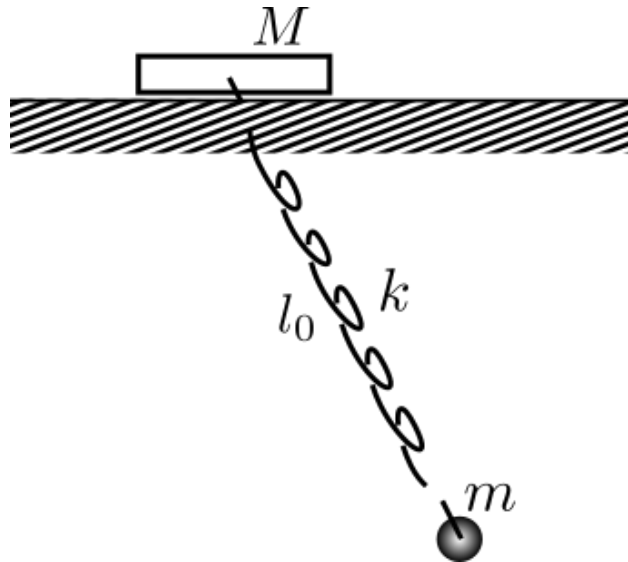
Problem 1. Three pendulums

Three identical pendulums are connected by the springs as shown on the figure. Find the normal modes



Problem 2. A pendulum a spring and a block

A ball of mass m is hanging on a weightless spring of spring constant k , which is attached to a block of mass M . The block can move along the table without friction. The length of the unstretched spring is l_0 . Find the normal modes of small oscillations.

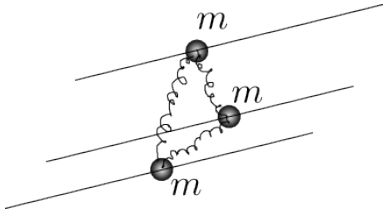


Problem 3.

Three infinite horizontal rails are at distance l from each other. Three beads of equal masses m can slide along the rails without friction. The three beads are connected by identical springs of constants k and equilibrium/unstretched length $l/2$.

1. Find the normal modes and the normal frequencies.

2. At time $t = 0$ one of the masses is suddenly given a velocity v . What will be the velocity of the whole system of three masses (average velocity) in the long time?



Homework 12. Due Wednesday, April 19

Problem 1.

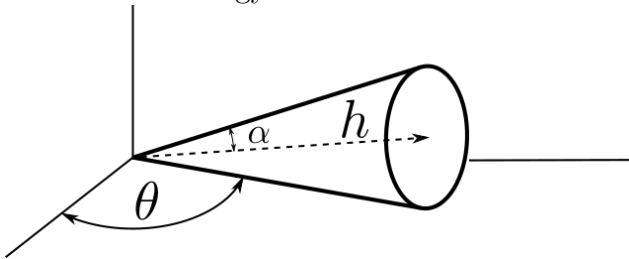
Determine the normal/eigen frequencies for two equal masses m on a ring of radius R . The masses are connected by two identical springs of spring constant k along the ring. The ring is in the vertical plane. The acceleration of the free fall is g . Consider only the case of hard springs: $\frac{mg}{kR} \ll 1$.

Problem 2.

1. Find the principal moments of inertia for a uniform stick of length a and mass M with respect to its center of mass.
2. Find the principal moments of inertia for a uniform square of mass M and side a .
3. Find the kinetic energy of the uniform cube of mass M and side a rotating with angular velocity Ω around its large diagonal.
4. Find the principal moments of inertia of the uniform circular cone of height h , base radius R , and mass M with respect to its vertex.
5. The same for a uniform ellipsoid of mass M and semiaxes a , b , and c with respect to its center.

Problem 3.

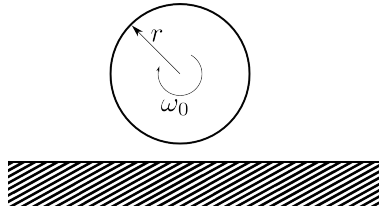
A cylindrical cone of mass M , height h , and angle α is rolling on the plane without slipping. Find its kinetic energy as a function of $\dot{\theta}$.



Homework 13. Due Wednesday, April 26

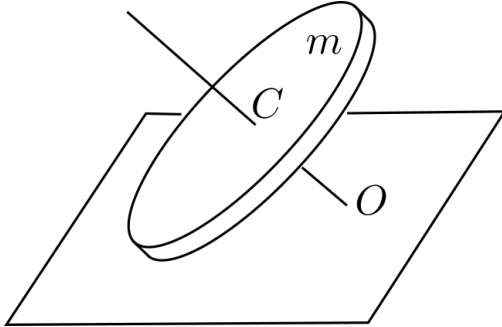
Problem 1. 1987-Fall-CM-G-6

A uniform solid cylinder of radius r and mass m is given an initial angular velocity ω_0 and then dropped on a flat horizontal surface. The coefficient of kinetic friction between the surface and the cylinder is μ . Initially the cylinder slips, but after a time t pure rolling without slipping begins. Find t and v_f , where v_f is the velocity of the center of mass at time t .



Problem 2. A coin

A uniform thin disc of mass m rolls without slipping on a horizontal plane. The disc makes an angle α with the plane, the center of the disc C moves around the horizontal circle with a constant speed v . The axis of symmetry of the disc CO intersects the horizontal plane in the point O . The point O is stationary. Find the kinetic energy of the disc.



Problem 3. A Rectangular Parallelepiped

A uniform Rectangular Parallelepiped of mass m and edges a , b , and c is rotating with the constant angular velocity ω around an axis which coincides with the parallelepiped's large diagonal.

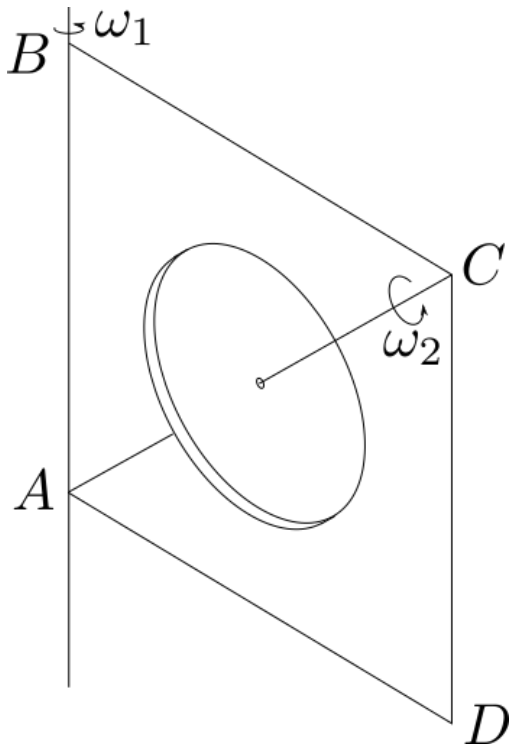
1. What is the parallelepiped's kinetic energy?
2. What torque must be applied to the axes in order to keep it still? (neglect the gravity.)

Problem 4. A disk in a frame

A square weightless frame $ABCD$ with the side a is rotating around the side AB with the constant angular velocity ω_1 . A uniform disk of radius R and mass m is rotating around the frame's diagonal AC with the constant angular velocity ω_2 . The center of the disk coincides with the center of the frame. Assuming $\omega_1 = \omega_2 = \omega$ find

1. The kinetic energy of the system.

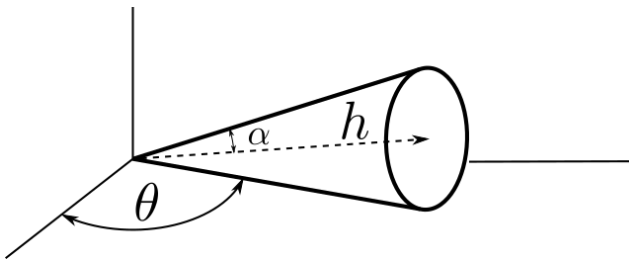
2. The magnitude of the torque that needs to be applied to the axes to keep it still.
(neglect the gravity.)



Problem 5.

A cylindrical cone of mass M , height h , and angle α is rolling on the plane without slipping.

1. Find its vector of angular momentum as a function of θ and $\dot{\theta}$ in the fixed system of coordinates.
2. Find the torque which acts on the cone.
3. Which force gives this torque?



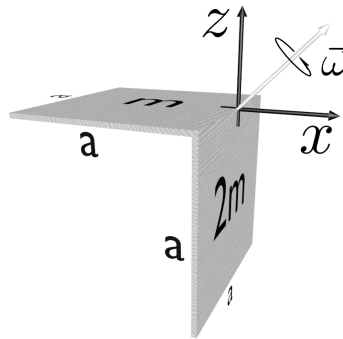
Homework 14. The last one. Due Wednesday, May 3

Problem 1. 2001-Spring-CM-G-4.jpg

A rotor consists of two square flat masses: m and $2m$ as indicated. These masses are glued so as to be perpendicular to each other and rotated about a an axis bisecting their common edge such that $\vec{\omega}$ points in the $x - z$ plane 45° from each axis. Assume there is no gravity.

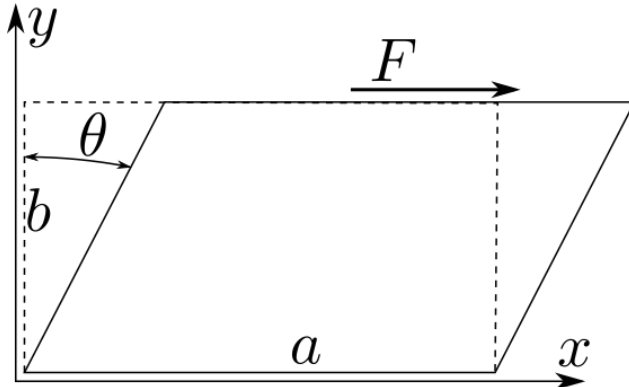
1. Find the principal moments of inertia for this rotor, I_{xx} , I_{yy} , and I_{zz} . Note that off-diagonal elements vanish, so that x , y , and z are principal axes.
2. Find the angular momentum, \vec{L} and its direction.
3. What torque vector $\vec{\tau}$ is needed to keep this rotation axis fixed in time?

Give all vectors in components of the internal $x - y - z$ system of coordinates.



Problem 2.

A parallelepiped with edges a , b , c was deformed as shown on the figure. Find the strain tensor in the linear approximation assuming that θ is small. Remember, the answer must be a 3×3 tensor.



Problem 3.

A cylinder of radius R and length L is squeezed by applying a uniform pressure P_0 to its end.

1. Find the change of length.
2. Find the change of the radius.

Express your results through Young's modulus E and Poisson ratio σ of the cylinder.

Problem 4.

A cylinder of radius R and length L is placed inside a very hard tube of the inner radius R and then squeezed by applying a uniform pressure P_0 to its end.

1. Find the change of length.
2. Find the pressure P the cylinder exerts on the tube.
3. What is the maximum possible P at given P_0 ?
4. What is the minimal possible P at given P_0 ? Hint: it's negative.

Express your results through Young's modulus E and Poisson ratio σ of the cylinder.